

CLAIMS

We claim:

- 1 1. A method for adjusting an m-bit CRC of a sub-message, wherein the CRC
2 generating polynomial is primitive or irreducible and the sub-message corresponds to
3 a composite sub-message having n trailing zeroes, comprising:
4 storing the m-bit CRC in an m-bit memory location;
5 examining each bit of N, where N equals $n \bmod (2^m - 1)$, in order from the
6 most significant bit to the least significant bit; the examining act for each examined
7 bit comprising:
8 finite field squaring the contents of the m-bit memory location, and;
9 if the examined bit equals one, advancing the contents of the m-bit
10 memory location to the next state as determined by the Galois field defined by the
11 CRC generating polynomial.
- 1 2. The method of claim 1, wherein the CRC generating polynomial is a primitive
2 polynomial.
- 1 3. The method of claim 1, wherein the CRC generating polynomial is an
2 irreducible polynomial
- 1 4. The method of claim 1, wherein for each examined bit equaling one, the finite
2 field squaring act and the advancing the contents act are performed simultaneously.

1 5. A method for adjusting an m-bit CRC of a sub-message, wherein the sub-
 2 message corresponds to a composite sub-message having n trailing zeroes and the m-
 3 bit CRC is equal or congruent to one, comprising:
 4 storing the m-bit CRC in an m-bit memory location;
 5 examining each bit of N, where N equals $n \bmod (2^m - 1)$, in order from the most
 6 significant bit to the least significant bit; the examining act for each examined bit
 7 comprising:
 8 finite field squaring the contents of the m-bit memory location, and;
 9 if the examined bit equals one, advancing the contents of the m-bit
 10 memory location to the next state as determined by the Galois field defined by the
 11 CRC generating polynomial.

1 6. The method of claim 5, wherein the CRC generating polynomial is neither
 2 primitive nor irreducible.

1 7. A method for adjusting an m-bit CRC of a sub-message, the sub-message
 2 corresponding to a composite sub-message having n trailing zeroes, wherein the CRC
 3 generating polynomial is $P(x)$, comprising:

- 4 (a) computing $Y = x^n \bmod P(x)$ using a lookup table;
- 5 (b) field multiplying the partial m-bit CRC and Y together; and
- 6 (c) field dividing the result from act (b) by $P(x)$, wherein the remainder forms
 7 the adjusted partial m-bit CRC.

1 8. The method of claim 7, wherein act (a) comprises:

- 2 (d) factoring x^n into powers of two;

- 3 (e) computing the modulus $P(x)$ of each factor from act (d) using a lookup
- 4 table, and
- 5 (f) computing Y by field multiplying together the results from act (e).

1 9. The method of claim 8, wherein $P(x)$ represents a 32 bit number and the
2 lookup table is no larger than 17 32-bit entries.

1 10. A method for adjusting an m -bit CRC of a sub-message, the sub-message
2 corresponding to a composite sub-message having n trailing zeroes, wherein the CRC
3 generating polynomial is $P(x)$ and n is less than m , comprising:

- 4 (a) computing $Y = x^n \bmod P(x)$ by setting $Y = x^n$;
- 5 (b) field multiplying the partial m -bit CRC and Y together by shifting the
- 6 partial m -bit CRC to the left by n bits; and
- 7 (c) field dividing the result from act (b) by $P(x)$, wherein the remainder forms
- 8 the adjusted partial m -bit CRC.

1 11. A method of adjusting a CRC of a message composed of a plurality of sub-
2 messages wherein the adjustment is in response to changes in a given sub-message,
3 the given sub-message having a first m -bit CRC and corresponding to a first
4 composite sub-message having n trailing zeroes, the changed sub-message having a
5 second m -bit CRC and corresponding to a second composite sub-message having n
6 trailing zeroes, and wherein the CRC generating polynomial is primitive or
7 irreducible, comprising:
8 storing the first m -bit CRC in a first m -bit memory location;
9 examining each bit of N , where N equals $n \bmod (2^m - 1)$, in order from the
10 most significant bit to the least significant bit; the examining act for each examined

11 bit comprising:
12 finite field squaring the contents of the first m-bit memory location,
13 and
14 if the examined bit equals one, advancing the contents of the first m-bit
15 memory location to the next state as determined by the Galois field defined by the
16 CRC generating polynomial, whereby the first m-bit memory location stores a third
17 CRC of the first composite sub-message;
18 modulo 2 subtracting the third CRC from the CRC of the message to produce
19 an intermediary CRC;
20 storing the second m-bit CRC in a first m-bit memory location;
21 examining each bit of N in order from the most significant bit to the least
22 significant bit; the examining act for each examined bit comprising:
23 finite field squaring the contents of the second m-bit memory location,
24 and;
25 if the examined bit equals one, advancing the contents of the second
26 m-bit memory location to the next state as determined by the Galois field defined by
27 the CRC generating polynomial, whereby the second m-bit memory location stores a
28 fourth CRC of the second composite sub-message;
29 modulo 2 adding the fourth CRC to the intermediary CRC to produce the
30 adjusted CRC of the message.

1 12. The method of claim 11, wherein the first and second memory locations are
2 the same.

1 13. The method of claim 11, wherein the CRC generating polynomial is primitive.

1 14. The method of claim 11, wherein the CRC generating polynomial is
2 irreducible.

1 15. A method of advancing an m-bit sequence through n states of a Galois field
2 generated by a primitive or irreducible polynomial of degree m, comprising:
3 storing the m-bit sequence in an m-bit memory location;
4 examining each bit of N, where N equals $n \bmod (2^m - 1)$, in order from the
5 most significant bit to the least significant bit; the examining act for each examined
6 bit comprising:
7 finite field squaring the contents of the m-bit memory location, and;
8 if the examined bit equals one, advancing the contents of the m-bit memory location
9 to the next state as determined by the Galois field.

1 16. The method of claim 15, wherein the polynomial is a primitive polynomial.

1 17. The method of claim 15, wherein the polynomial is an irreducible polynomial.